

Nuclear shadowing in ultrarelativistic heavy ion collisions

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Outline

In collaboration with:

L. Bravina, E. Zabrodin, I.C. Arsene, A.B. Kaidalov

1 Introduction

- Critical energy - coherence length
- Nuclear shadowing
- Inclusive and diffractive parton densities
- Model of multiple scattering

2 Results

- Nuclear parton distribution
- Relation to heavy ion experiment

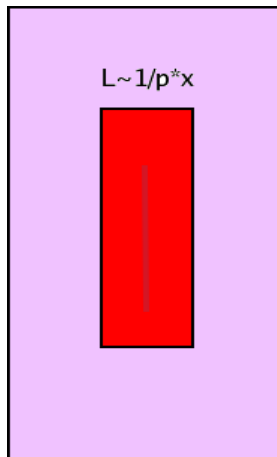
3 Summary



Space-time picture of nuclear interactions I

Feynman, Gribov...

- a fast-moving hadron or nucleus can be considered as a complicated fluctuation of quarks and gluons with long lifetimes
- content of the state is Lorentz-frame dependent
- fast parton components of the wave function are Lorentz-contracted, while soft ones are not



Space-time picture of nuclear interactions II

When the **coherence length** (“longitudinal size”) of the fluctuation becomes as large as the target nucleus, the space-time picture of particle production changes. For typical processes:

Critical energy

$$E_C \sim m_N^2 R_A$$



$$x < 1/(m_N R_A)$$

When $x > 1/(m_N R_A)$, the space-time picture is that of final state reinteractions of produced particles with formation time (longitudinal structure).



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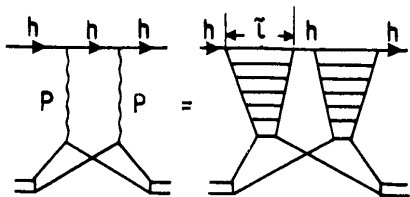
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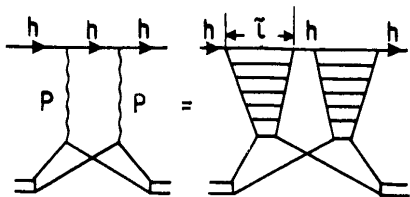
“Planar” diagram

- low energy scattering - longitudinal ordering
 - Glauber multiple scattering
- high energy scattering - change in initial condition
 - planar diagrams $\sim 1/E$
 - fluctuation prepared long before the collision
- discontinuities of non-planar diagrams determined by AGK cutting rules

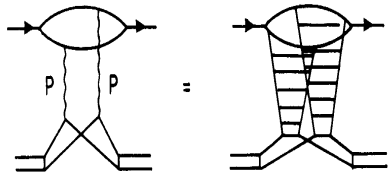


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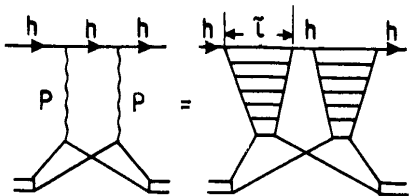
“Non-planar” diagram

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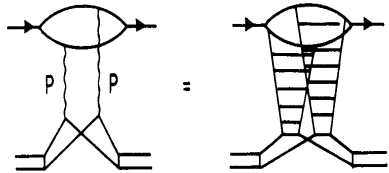


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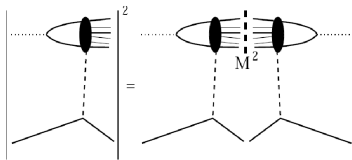
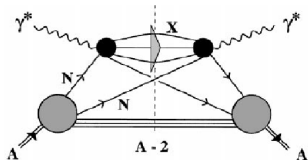
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Gribov inelastic shadowing

Correction to Glauber model

We need to sum up all possible planar and non-planar diagrams, how...



- Glauber model is still ok, but...
- take into account **inelastic** intermediate states, but..
- space-time picture does not correspond to successive rescatterings!
- **AGK cuttings** $1 + (-4) + 2 = -1$

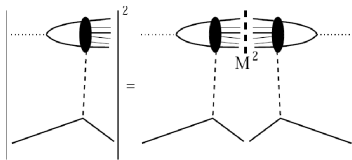
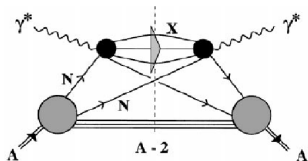
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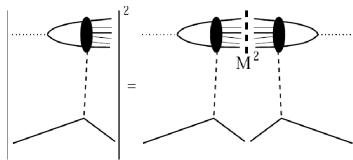
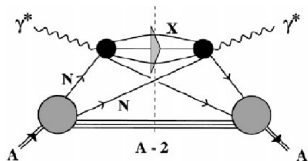
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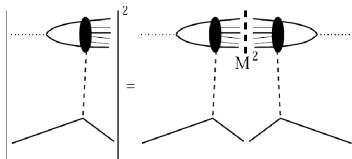
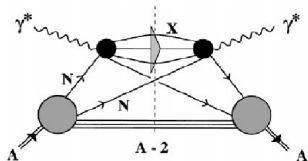
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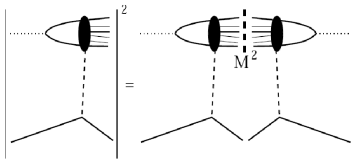
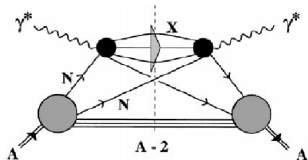
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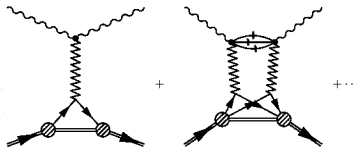


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Multiple scattering series



- The contribution from 1, 2... scatterings can be expanded in

$$\sigma_A = \sigma_A^{(1)} + \sigma_A^{(2)} + \dots$$

$$\sigma_A^{(1)} = A \cdot \sigma_N,$$

$$\sigma_A^{(2)} = -4\pi A(A-1) \int d^2b T_A^2(b) \int_{M_{min}^2}^{M_{max}^2} dM^2 \left[\frac{d\sigma_{\gamma^*N}^D(Q^2, x_P, \beta)}{dM^2 dt} \right]_{t=0} F_A^2(t_{min})$$

Armesto et al. Eur.Phys.J.C **29** (2003) 531



Second order rescattering

Relation to diffractive DIS

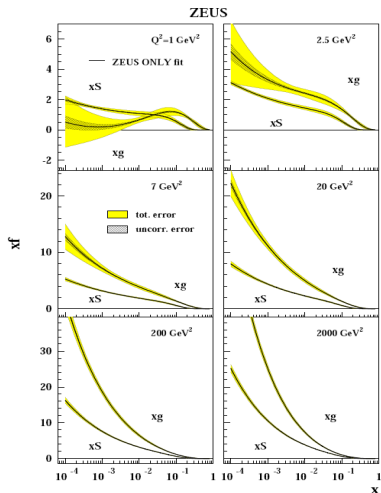
$$\sigma_A^{(2)} = -4\pi A(A-1) \int d^2b T_A^2(b) \int_{M_{min}^2}^{M_{max}^2} dM^2 \left[\frac{d\sigma_{\gamma^* N}^{\mathcal{D}}(Q^2, x_P, \beta)}{dM^2 dt} \right]_{t=0} F_A^2(t_{min})$$

- F_A : nuclear form factor
- $T_A(b)$: nuclear density profile
- dM^2 : integration over the diffractively produced hadronic system
 - M_{min}^2 : minimal mass of produced system
 - M_{max}^2 : large rapidity gap is required ($x_P^{max} \ll 1$).



Parameterization of parton densities in proton

Inclusive cross-section



ZEUS Collaboration, PRD **67** (2003) 012007

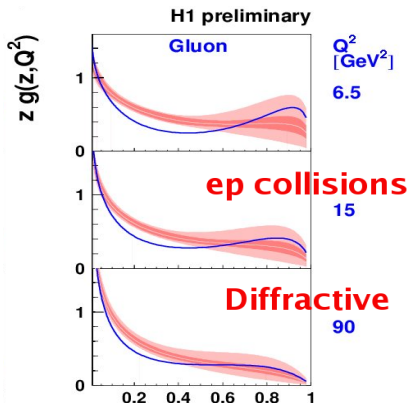
$$\sigma_{\gamma^* N} = \frac{4\pi^2\alpha_{em}}{Q^2} F_2(x, Q^2)$$

- Q^2 evolution given by pQCD **DGLAP**
- several parameterizations on the market
- **Online:**
<http://durpdg.dur.ac.uk/hepdata>
- we use **CTEQ6**



Parameterization of parton densities in the Pomeron

Diffractive cross-section



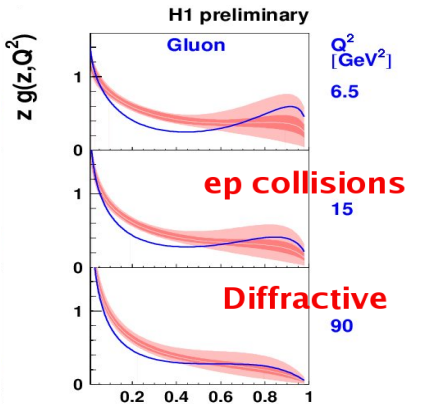
$$\left[\frac{d\sigma_{\gamma^* N}^D}{dM^2 dt} \right]_{t=0} = \frac{4\pi^2 \alpha_{em} B}{Q^2(Q^2 + M^2)} X_P F_{2D}^z$$

H1 Collaboration, paper **980** at ICHEP2002



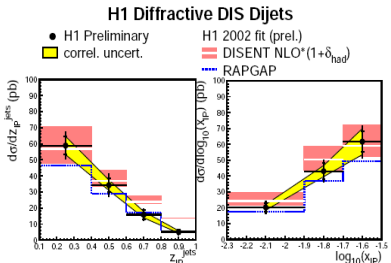
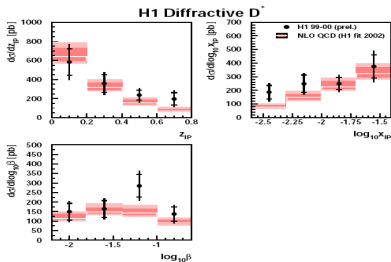
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Diffractive cross-section



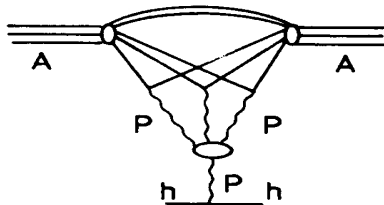
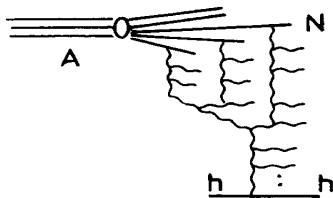
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H1 Collaboration, paper 980 at ICHEP2002



Enhanced diagrams

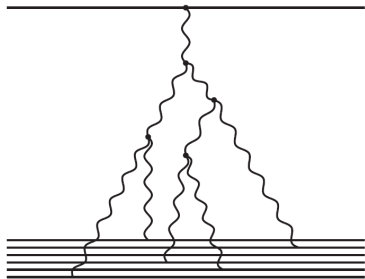
Interactions between parton ladders/Pomerons



- soft partons from different ladders overlap and start to interact
- 3P and 4P vertexes are rather small
- become important for hA ($A^{1/3}$) and AB ($A^{1/3} + B^{1/3}$) collisions and at high energies
- related to **saturation** of (gluon) densities in ultrarelativistic nuclear reactions - gluon fusion, Pomeron loops



Schwimmer summation of fan diagrams



Schwimmer Nucl.Phys.B **94** (1975) 445

- splittings of Pomerons
- exact solution of Regge field theory
- similar results as with quasi-eikonal model
- works for hA scattering
- describes a "saturation" of the cross section

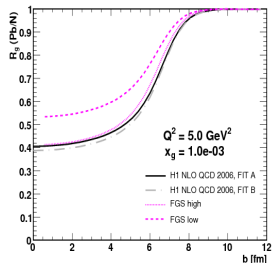
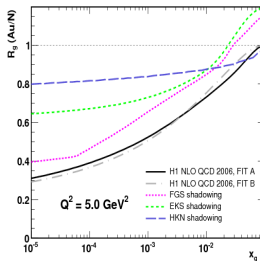
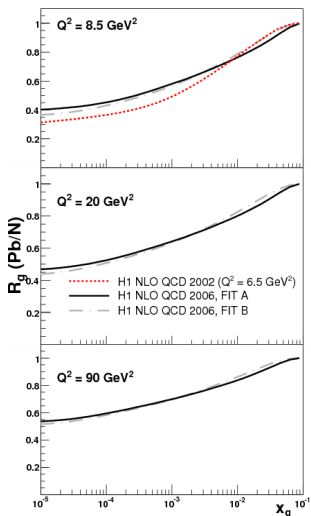
$$\sigma_{hA}^{Sch} = \sigma_{hN} \int d^2b \frac{AT_A(b)}{1 + (A-1)f(x, Q^2)T_A(b)},$$

$$f(x, Q^2) = 4\pi \int_x^{x_P^{max}} dx_P B(x_P) \frac{F_{2D}^{(3)}(x_P, Q^2, \beta)}{F_2(x, Q^2)} F_A^2(t_{min.})$$



Gluon and sea quark shadowing

Details - PLB 657 (2007) 170



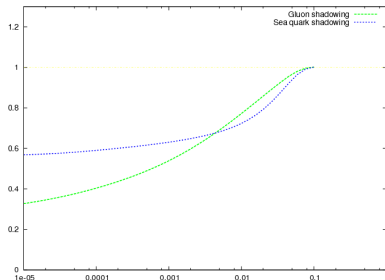
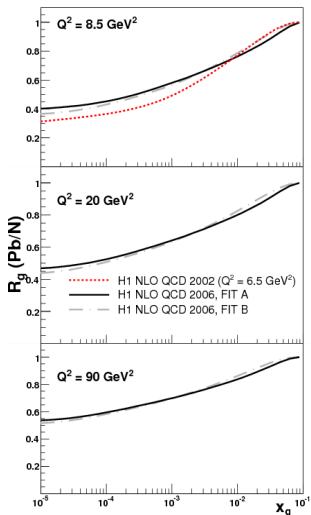
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- strong shadowing obtained
- no fitting or free parameters!



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Nuclear interactions at high energies

Corrections to the Glauber formula

Due to **AGK** all rescatterings cancel at mid-rapidity and $s \rightarrow \infty$!

Density of charged particles

$$\frac{dn_{AB}^a(b)}{dy} = \frac{T_{AB}(b) \sigma_{pp}^{inel}}{\sigma_{AB}^{inel}} \frac{dn_{NN}^a}{dy}$$



Shadowing correction!

$$\frac{dn_{AA}^a(b)}{dy} = \frac{T_{AB}(b) \sigma_{pp}^{inel}}{\sigma_{AB}^{inel}} \frac{dn_{NN}^a}{dy} R(A/N)R(B/N)$$

For RHIC a decrease of particle densities by a factor ~ 2 , for LHC ~ 4
 - agrees with experiment!

Capella, Kaidalov, Van; Heavy Ion Phys. **9** (1999) 169



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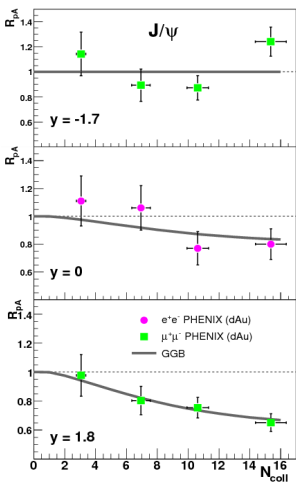
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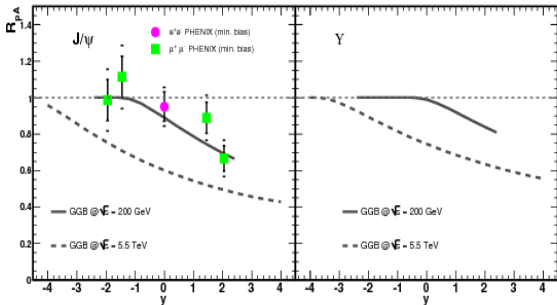


Example: J/ψ production in hA @ RHIC and LHC

arXiv:0711.4672 [hep-ph], arXiv:0708.3801 [hep-ph]

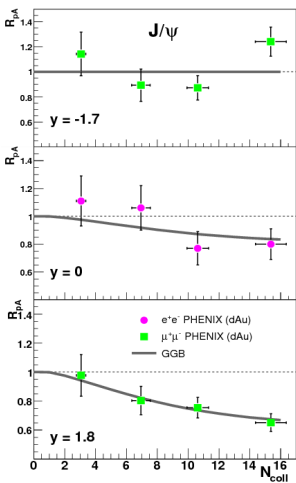


- shadowing in agreement with data at RHIC
- first signal of coherent HQ production?
 - at LHC - strong IS effect!

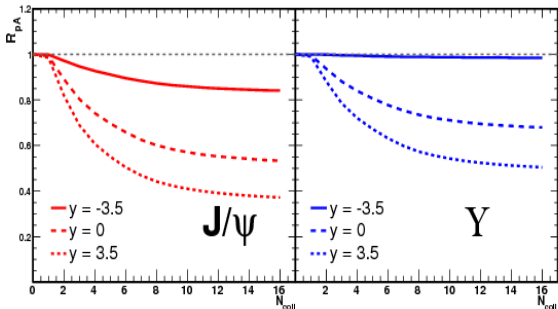


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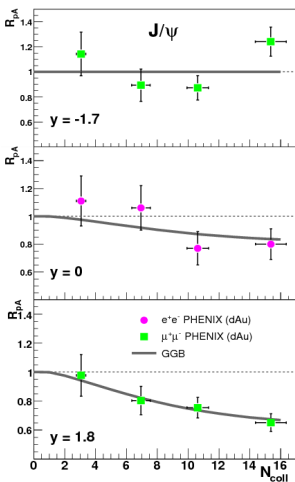


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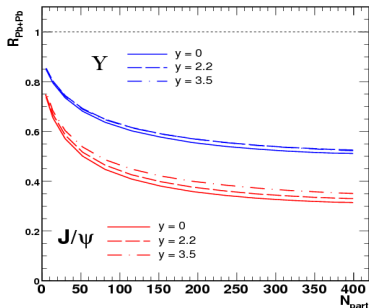


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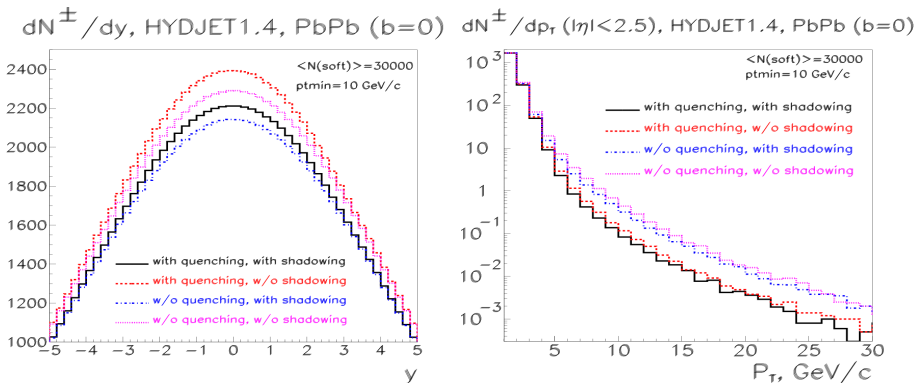


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Example: Predictions for LHC

Rapidity and p_T spectra of charged particles



Rapidity and p_T spectra of charged hadrons in Pb+Pb collisions at LHC energy $\sqrt{s} = 5.5 \text{ TeV}$. Quenching and shadowing is only for the hard part, $\langle N(\text{soft}) \rangle$ is a free parameter.



Summary

- Nuclear shadowing was calculated in the Gribov approach
- Large shadowing corrections both for gluons and sea quarks are found from diffractive data
- No parameters were fitted in the model
- Shadowing leads to a substantial drop of particle densities in heavy-ion collisions compared to the simple Glauber model
 - visible e.g. in d+Au collisions at RHIC (J/ψ , high- p_{\perp} production)
 - crucial in nucleus-nucleus collisions at RHIC and LHC!
- Essential tool for the study of hadronic matter at extreme conditions
 - high density quark-gluon systems in deconfined phase



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